



COMPLEX SYSTEMS, NETWORKS AND SPACE

Cazabet Rémy

gopro2017 : Spatial Optimized Designs: from Cities to Natural systems

WHO AM I

- Maître de conférences (since September) in Computer Science (LIRIS, Lyon I)
- Traditional topics:
 - ▶ “Network Science”
 - Network Analysis, Network Mining, “Community Detection”, Dynamic Networks, etc.
 - ▶ “Data Science”
 - Learning knowledge from data
 - ▶ “Complex Systems”
 - Systems composed of multiple parts in interaction, non-linear behaviour, cannot be studied by reductionism:
 - Interactions between entities => Network

CITIES ? NATURAL SYSTEMS ?

- Cities and natural systems are complex systems
- 2015-2016: Working on Vél'innov ANR Project: understanding, characterising activity in Bike Sharing Systems (BSS)
- Currently: starting a collaboration with Claire Lesieur on the organisation of proteins

ORGANISATION OF COMPLEX SYSTEMS

- Usually, there is not **one** network of a complex system:
 - ▶ In cities:
 - Network of proximity between buildings
 - Network of trips using public transportations
 - Network of trips using bicycle
 - Network of roads
 - Network of socio-demographic similarities
 - Network of phone calls between neighbourhoods
 - ...
 - ▶ Each dataset can be modelled by countless networks, using thresholds, temporal aggregations, etc.
 - ▶ I'm not working on a network in particular, just networks as models of interactions inside complex systems (Complex networks ?)

ORGANISATION OF COMPLEX SYSTEMS

- Complex Networks are not random. They have a particular **organisation**.
- My ultimate goal is to understand this organisation.
 - Find underlying rules explaining difference between observed and random networks
 - **Spatial organisation** is one potential **candidate** to explain the structure of networks

NETWORK & SPACE

- What is a spatial network model:
 - ▶ Nodes are characterised by a position, i.e an x -dimensional vector
 - ▶ The probability of observing an edge depends on the distance between nodes

NETWORK & SPACE

- Networks and spatial organisation have a complex history
 - ▶ First network models were often spatial-like:
 - Regular grids (nodes on a grid, edges at fix distance)
 - Watts-strogatz (nodes on a circle, most edges depends on distance)
 - ▶ Later models often have no spatial structure
 - Community-based
 - Dynamic models (preferential attachment, forest fire, ...)
 - ▶ Most network representations are based on 2D projections
 - ▶ The come back of spatial organisation: network embedding.
 - Given a network, which position of nodes better explain its organisation ?

AN EXAMPLE: VÉLO'V

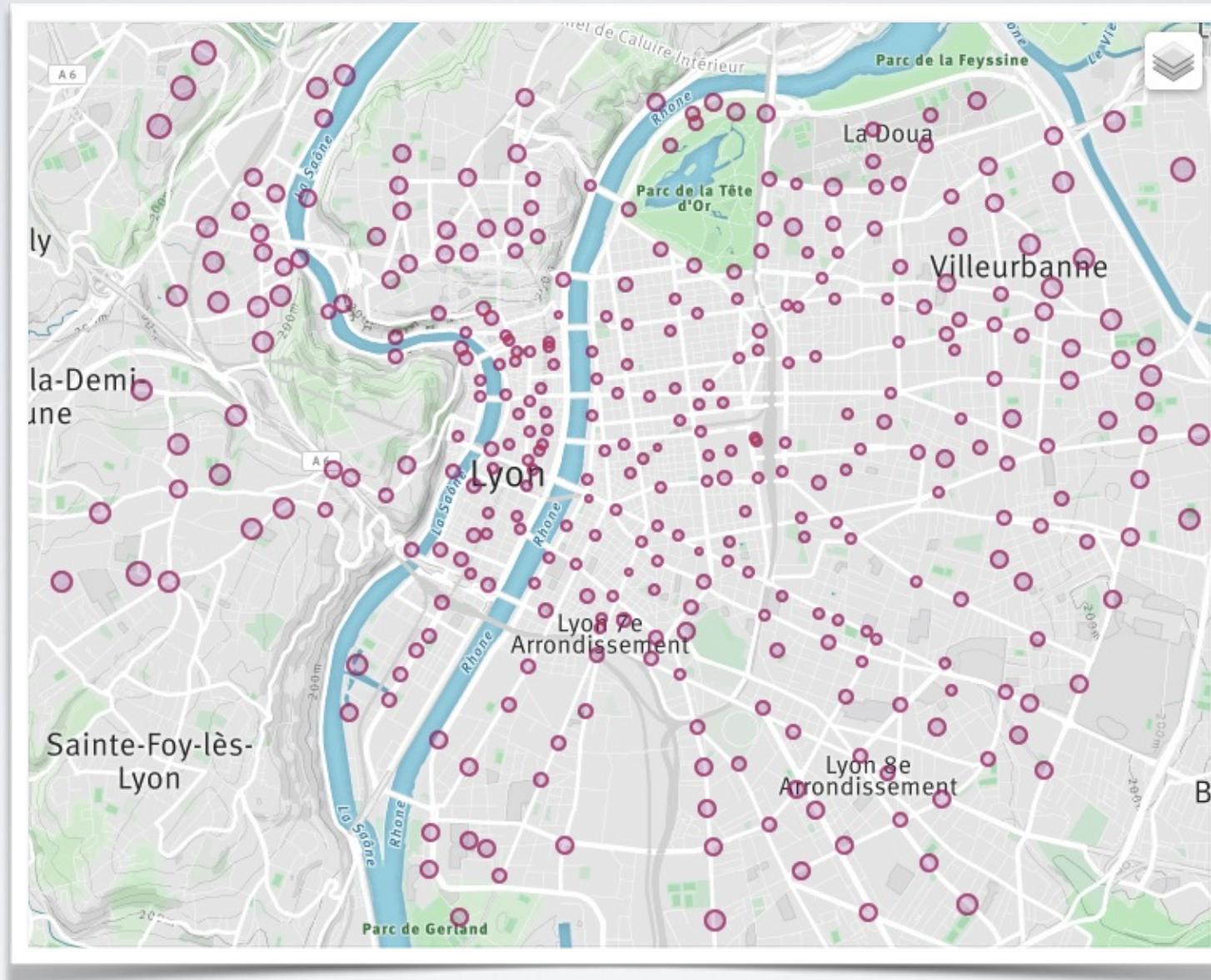
VÉLO'V



Bicycle Sharing System (BSS) in Lyon

Dataset: trips (5y) + sociodemographic around stations

VÉLO'V



Nodes: station (2D position)
Edges: number of trips over a period

NETWORK MODEL I

- Random network
- #trips between any pair of station is the same

$$p_{ij}^{RR} = \frac{1}{m}$$

Model complexity:

|

Model precision:

+

Evaluation of the model :
diff between observed network and model

NETWORK MODEL 2

- Configuration model
- #trips between any pair of station depends on their “popularity”

$$P_{ij}^{Conf} = k_i k_j W$$

Model complexity:

n

Model precision:

++

NETWORK MODEL 3

- Simple Gravity
- #trips between any pair of station depends on their “popularity” and their distance

Model complexity:

$$n+2n$$

Model precision:

++++

$$P_{ij}^{Grav2} = W \frac{k_i k_j}{d_{ij}^2}$$

NETWORK MODEL 4

- Gravity with custom deterrence function
- #trips between any pair of station depends on their “popularity” and their distance.
- Distance influence learnt from data

Model complexity:

$$n+2n+a$$

Model precision:

++++

$$P_{ij}^{Grav2} = Wk_i k_j f(d_{ij})$$

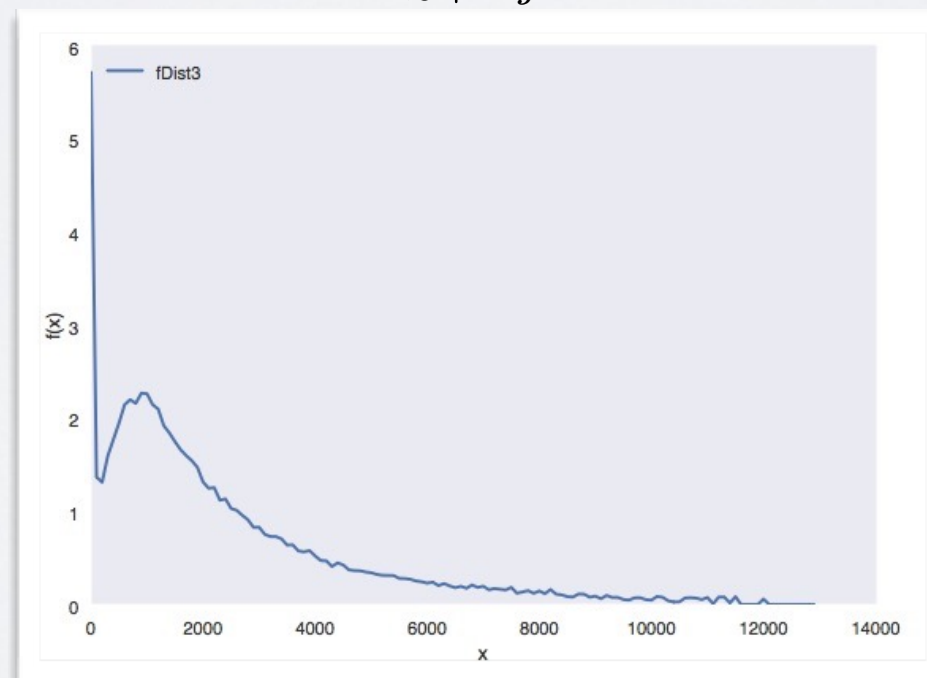
DETERRENCE FUNCTION

Computation of a deterrence function:
Impact of distance on edge probability

(Comparing observation with Configuration Model)

$$f(d) = \frac{\sum_{i,j|d_{ij}=d} A_{ij}}{\sum_{i,j|d_{ij}=d} N_i N_j}$$

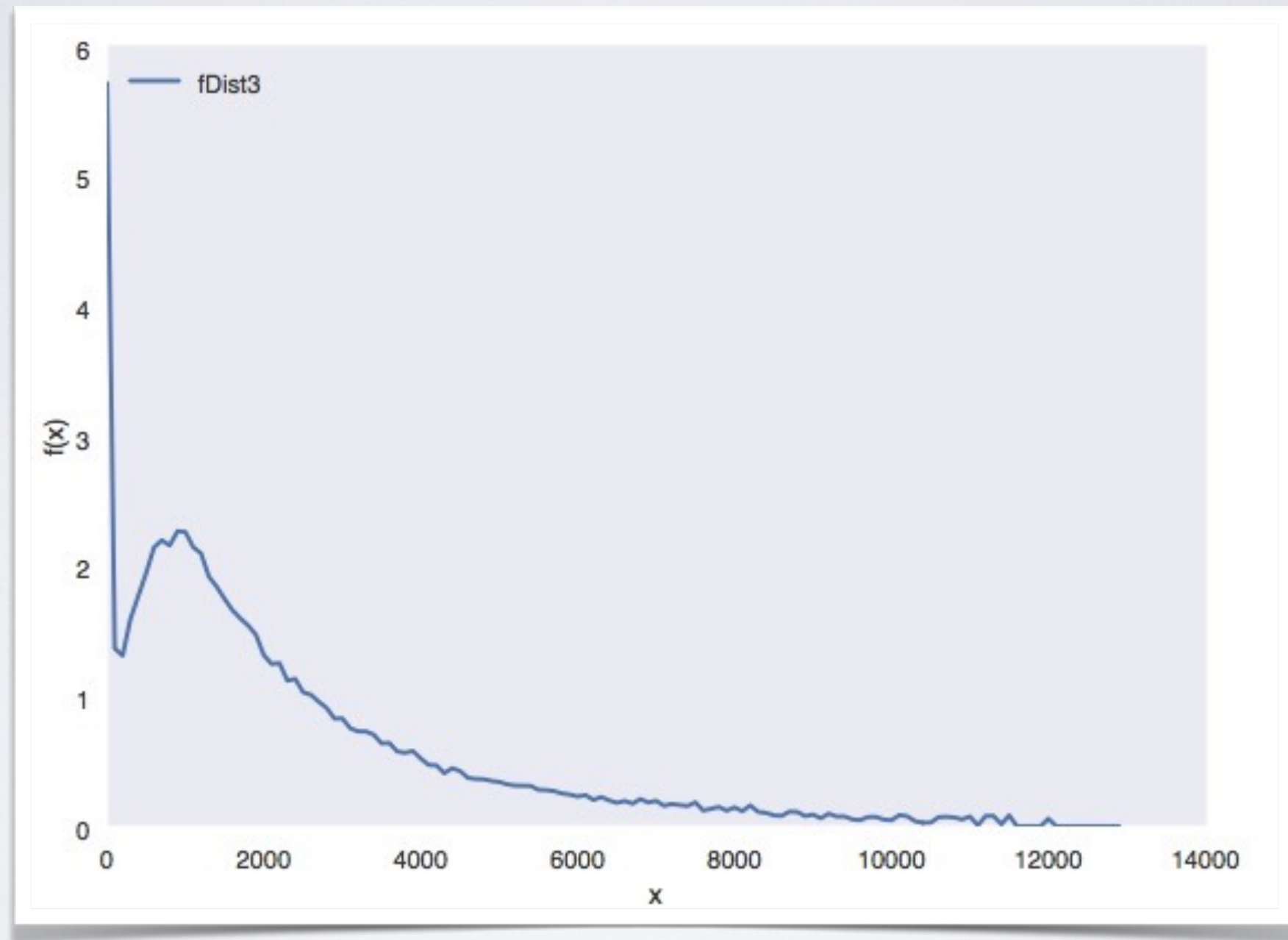
$f(d)$



Distance d (meters)

DETERRENCE FUNCTION

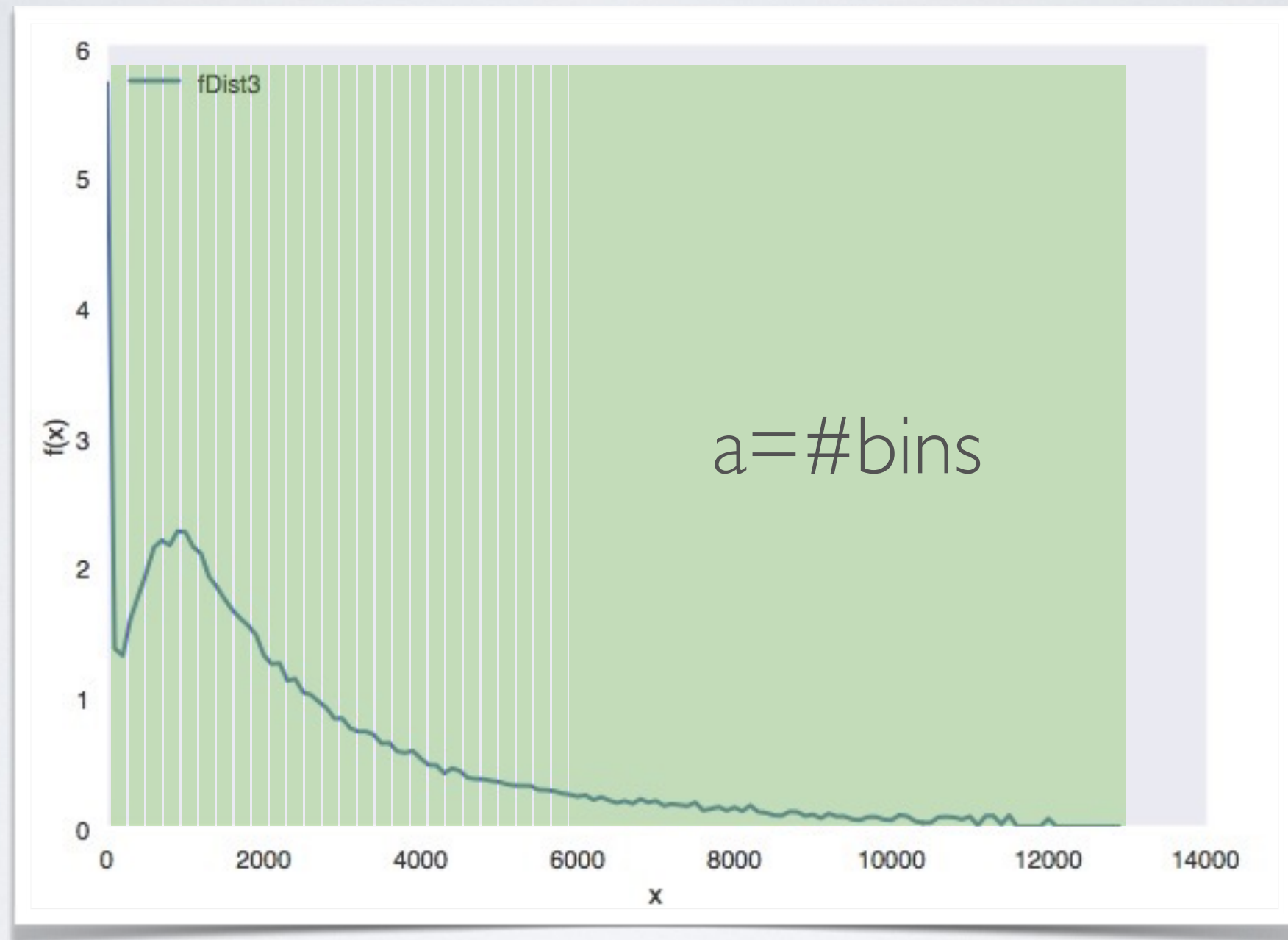
$f(d)$



Distance d (*meters*)

DETERRENCE FUNCTION

$f(d)$



Distance d (*meters*)

NETWORK MODEL 4

- Gravity with custom deterrence function
- #trips between any pair of station depends on their “popularity” and their distance.
- Distance influence learnt from data

Model complexity:

$$n+2n+a$$

Model precision:

++++

$$P_{ij}^{Grav2} = Wk_i k_j f(d_{ij})$$

NETWORK MODEL 5

- Gravity with custom deterrence function and conservation of degrees
- Same as before, but constraint to conserve node degrees

Model complexity:

$$n+2n+a$$

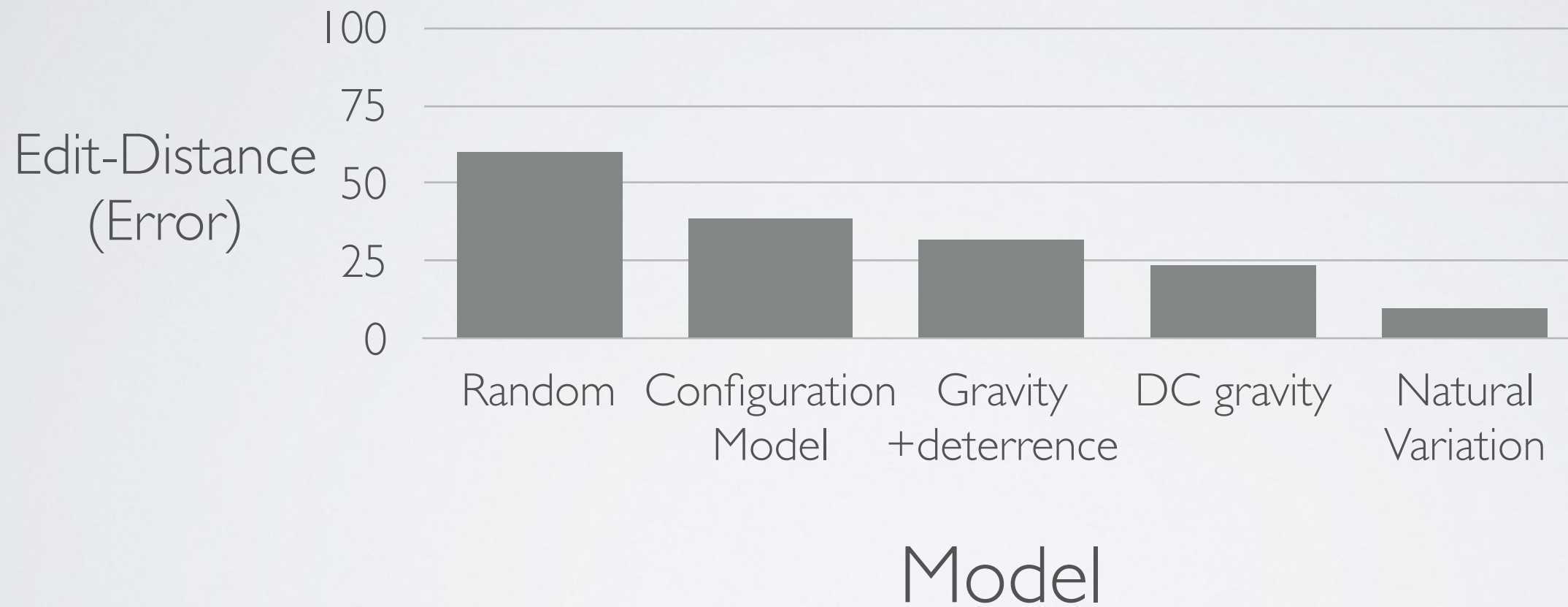
Model precision:

$$+++++$$

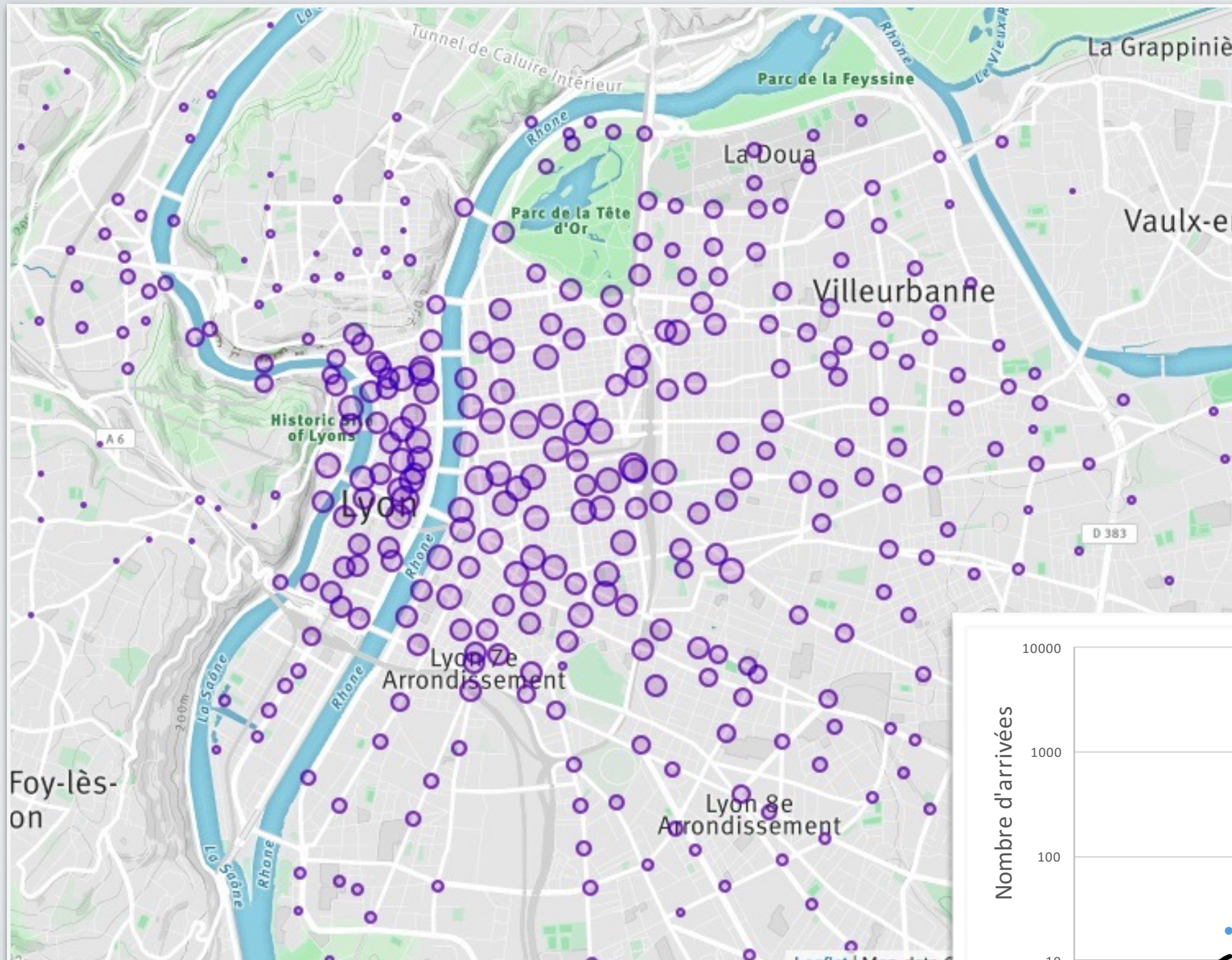
$$P_{ij}^{DCgrav} = n^{Oeis} n^{Ieis} f(d_{ij})$$

$$n^{Ieis} = \frac{deg^{out}(i)}{\sum_i n^{Oeis} f(d_{ij})}, n^{Oeis} = \frac{deg^{in}(i)}{\sum_i n^{Ieis} f(d_{ij})}$$

MODEL EVALUATION

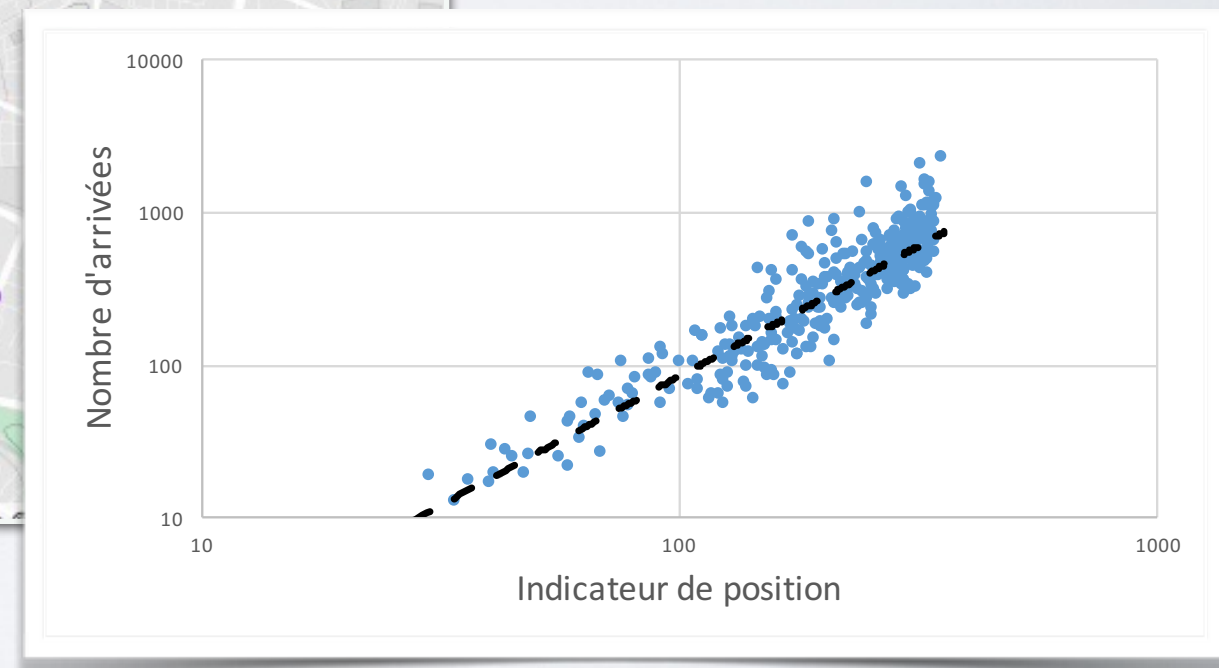


USEFUL MODEL ?



Geographic Potential P_i

$$P_i = \sum_j f(d(i,j))$$

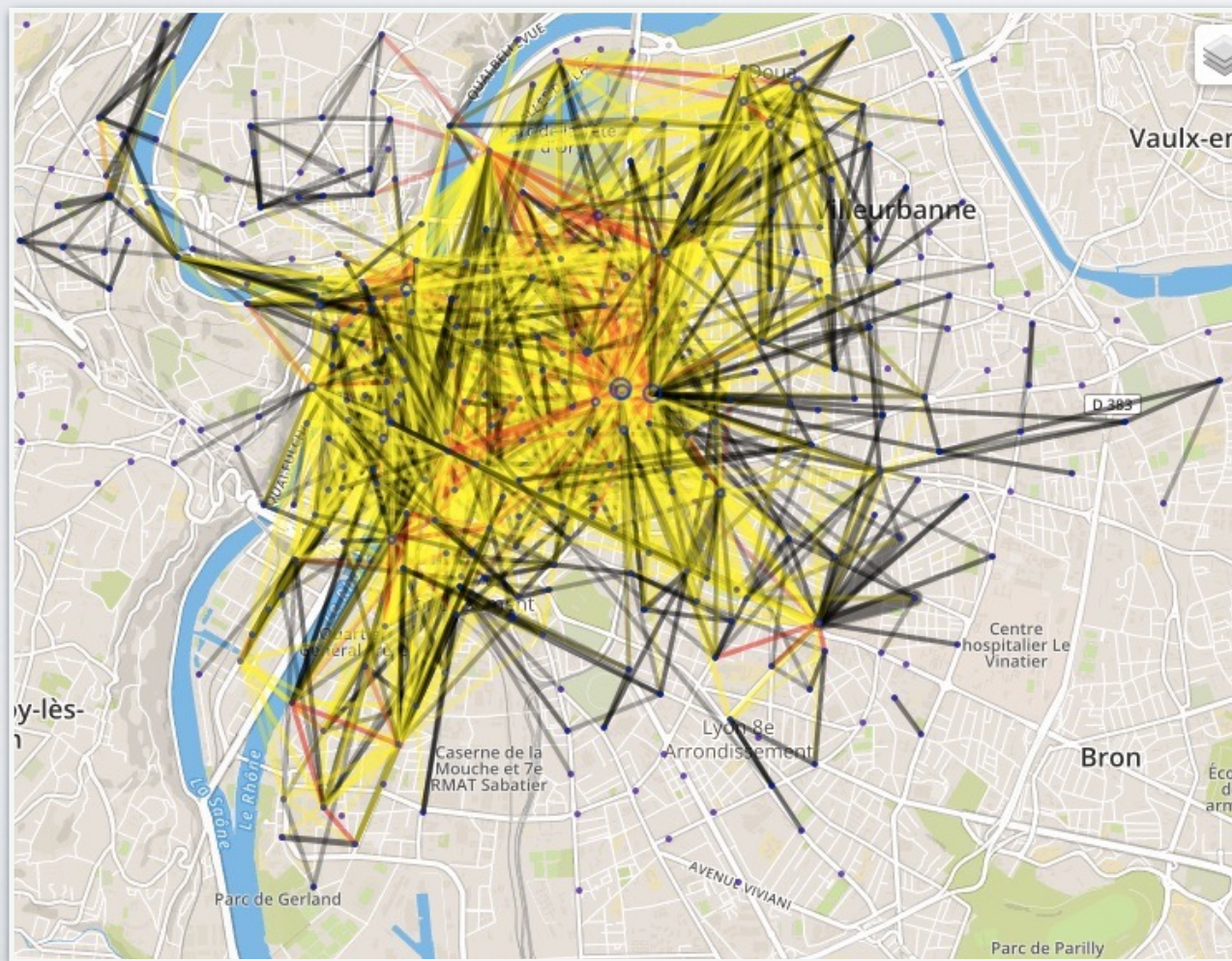


IMPROVING THE MODEL ?

- Difference between observed network and model. Random errors ?

IMPROVING THE MODEL ?

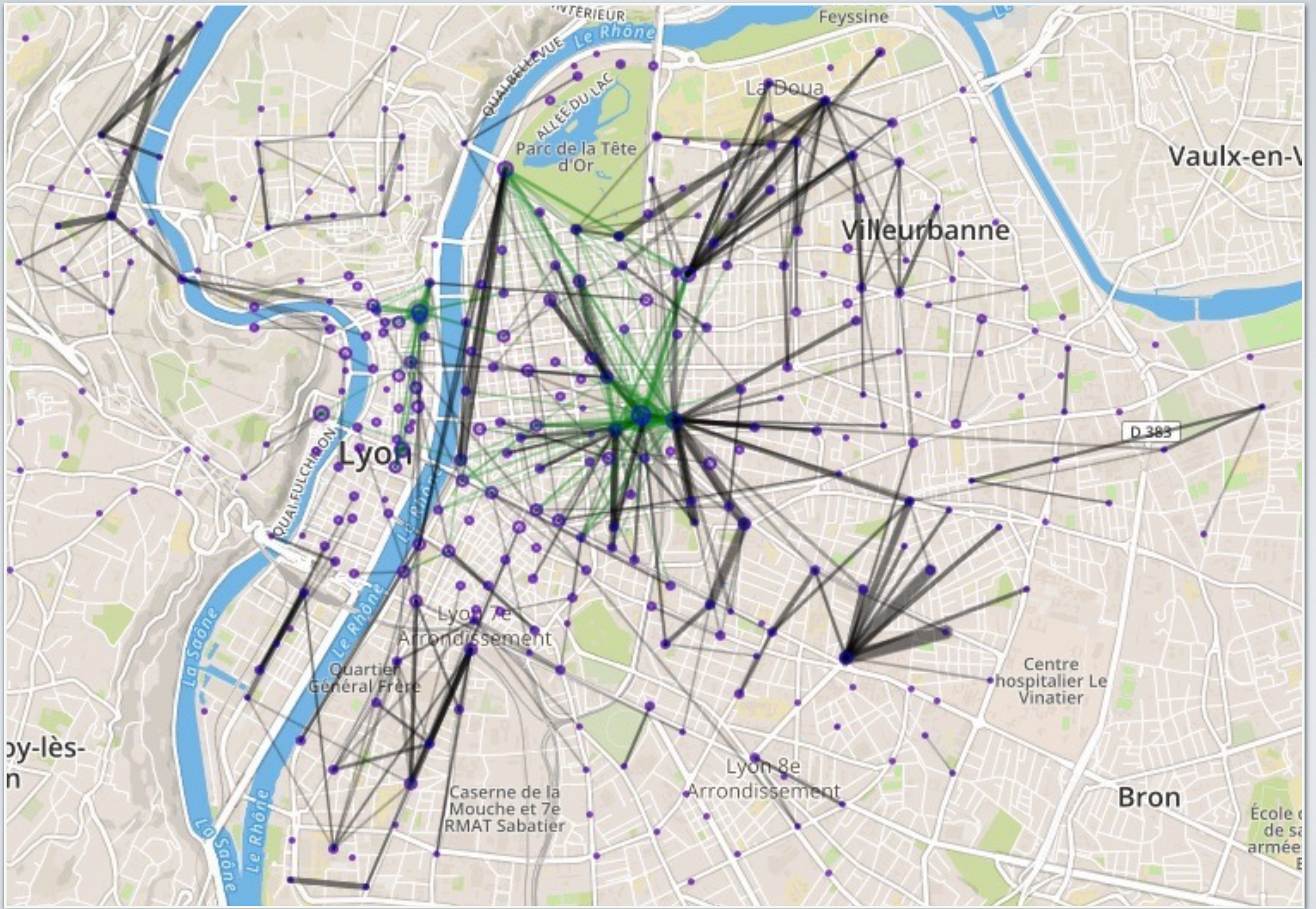
- Difference between observed network and model. Random errors ?



Yellow: well predicted

Red: overestimated

Black: Underestimated



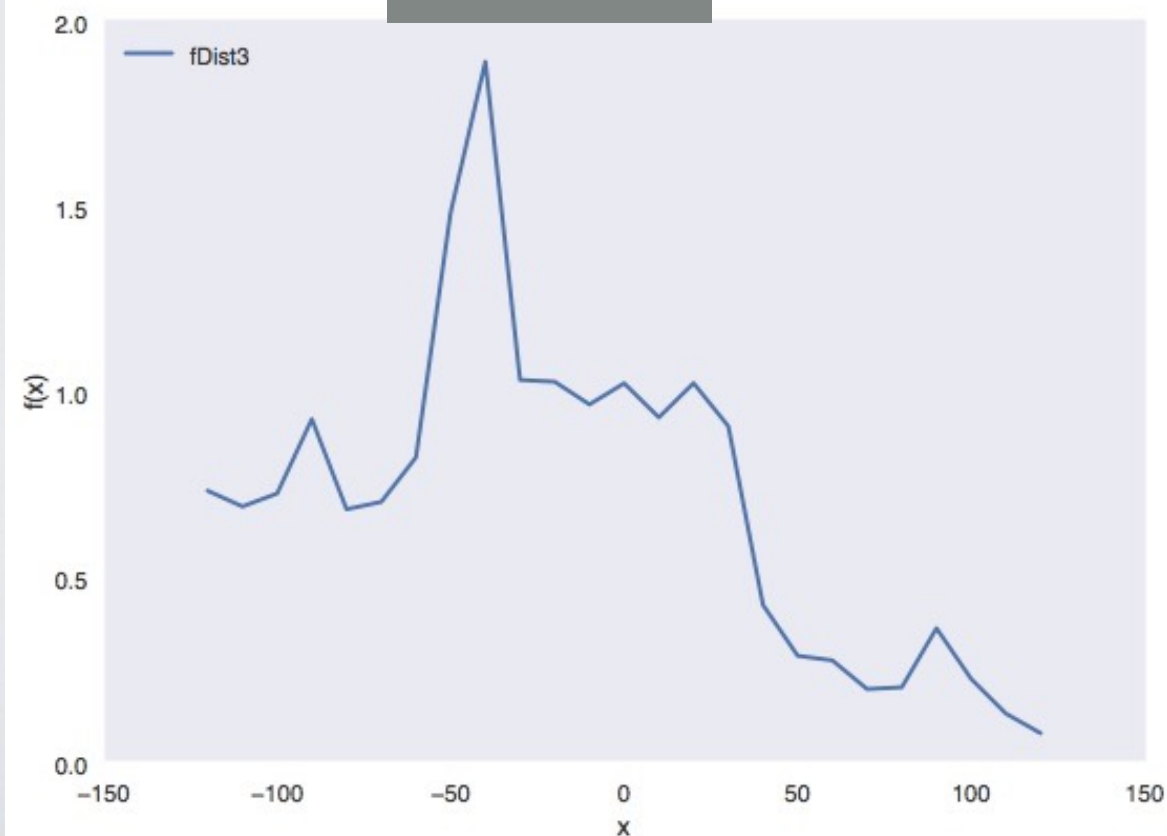
MODEL OF IST MODEL ERRORS ?

- Incorrectly predicted trips constitute a new network
 - ▶ Cannot be modelled by geographical gravity model (flat deterrence func)
 - ▶ Socio-demographic gravity model ?
 - ▶ Community structure ?

NON-GEOGRAPHICAL GRAVITY MODELS

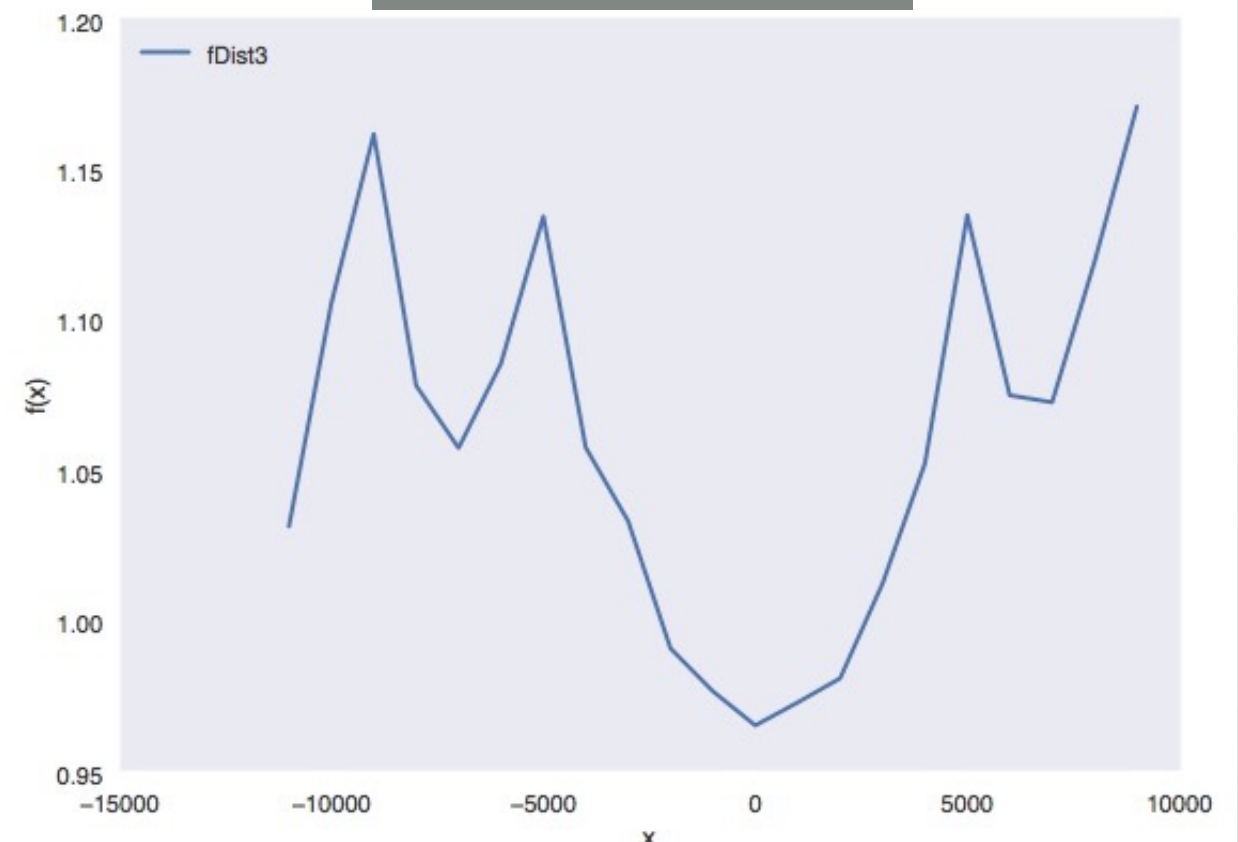
- Deterrence function can be computed on any distance function (here, on top of spatial effect)

Altitude



Altitude difference (meters)

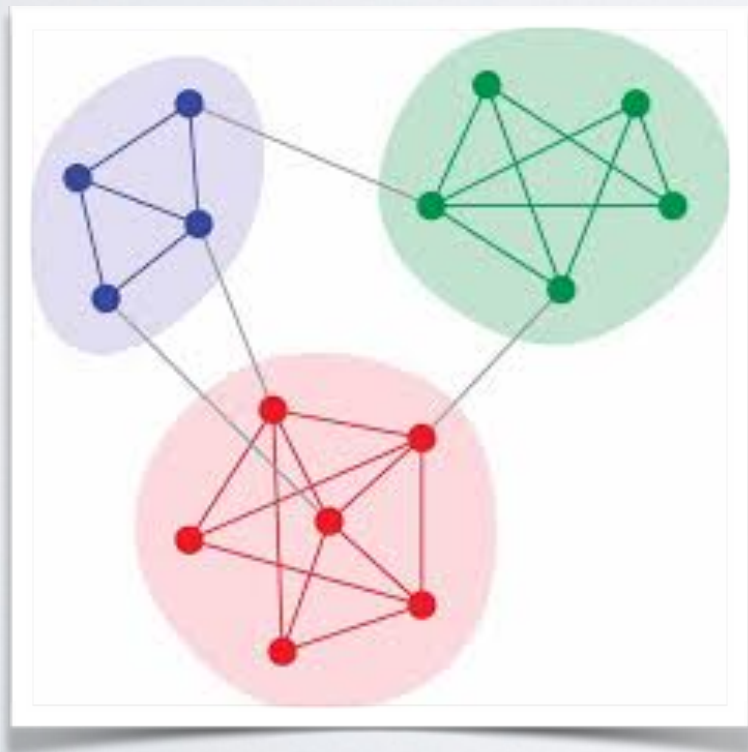
Job difference



Job difference (#job)

COMMUNITY STRUCTURE

- Community discovery (or graph clustering, SBM...)
 - Searching for groups of nodes with similar connections behaviours
 - Often dense groups less connected to the rest of the network, but not always



Community graph model:

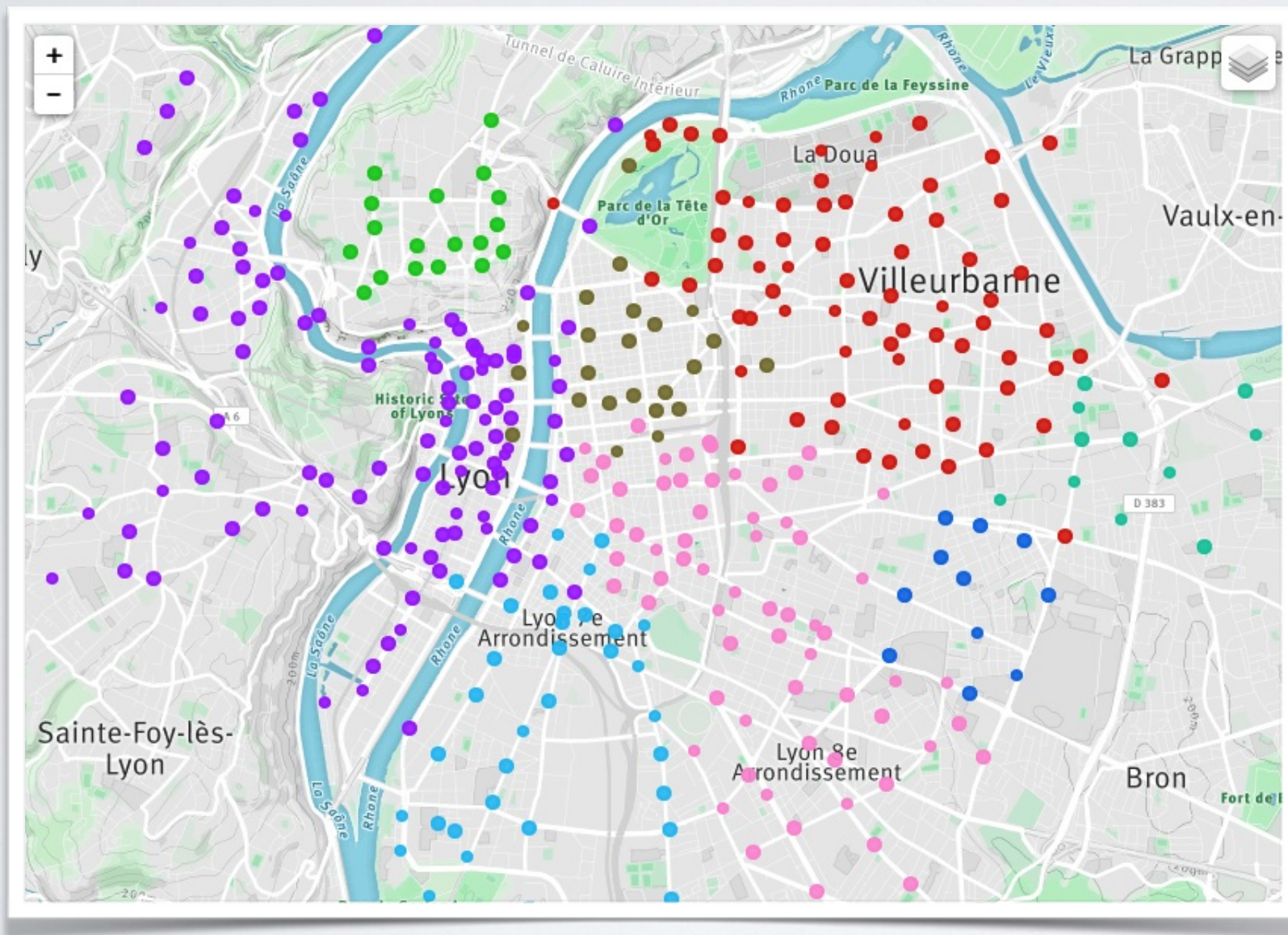
Simple

$$P_{ij}^{SBM} = W p^c(c_i, c_j)$$

Degree-Corrected

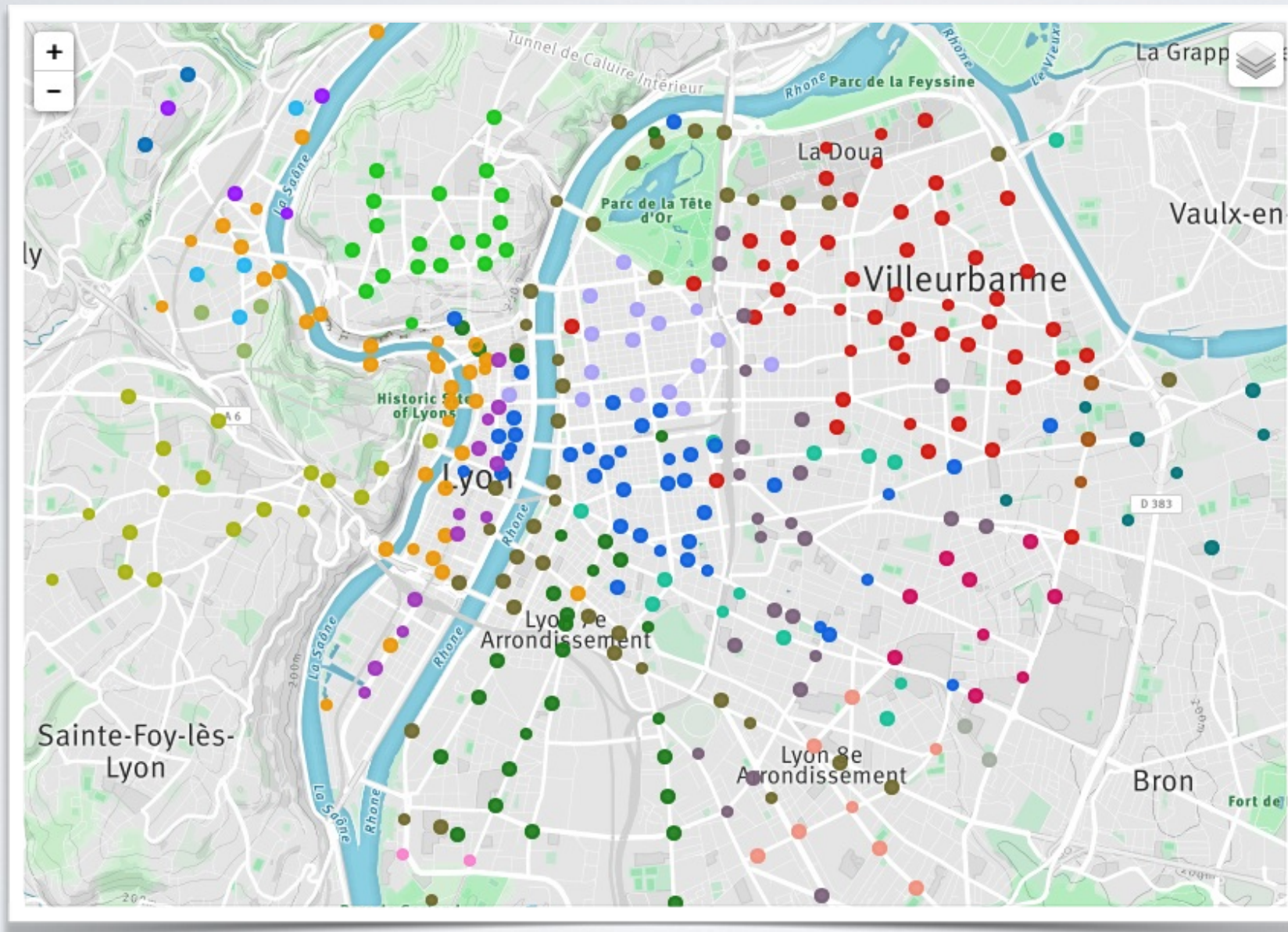
$$P_{ij}^{DC-SBM} = W k_i k_j p^c(c_i, c_j)$$

COMMUNITY STRUCTURE



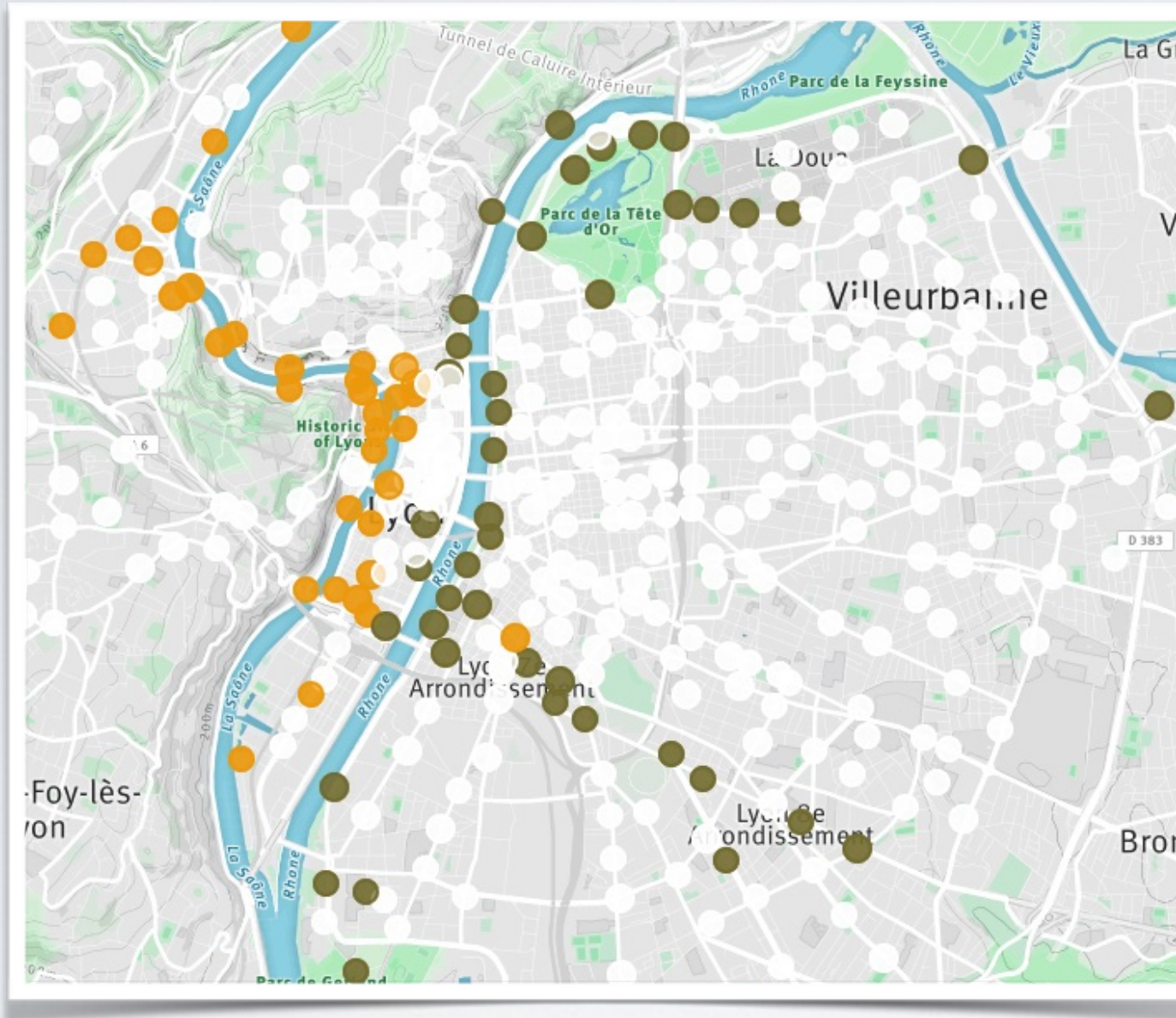
Community
Structure
of the
Original
Network

COMMUNITY STRUCTURE



Community
Structure
Of trips
Unexplained
By Spatial Model

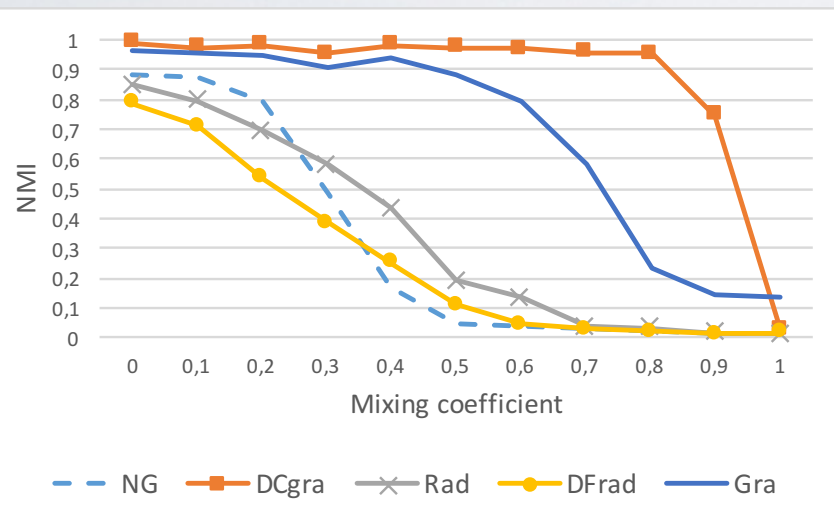
COMMUNITY STRUCTURE



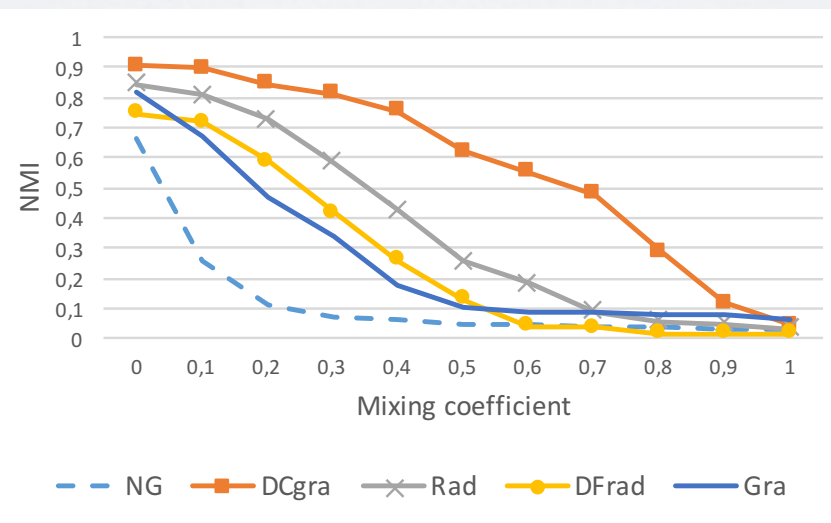
Community
Structure
Of trips
Unexplained
By Spatial Model

MIXED MODELS ?

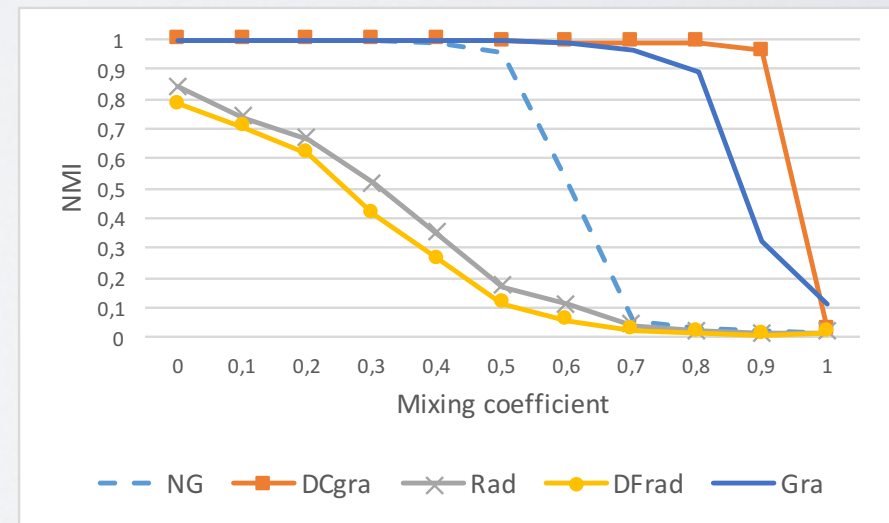
- Validation on synthetic cases:
 - Generation of networks with both a spatial and community structure.
 - Can we discover both of them ?



(b) $f(x) = 1/x$, N/P Only



(d) $f(x) = 1/x^2$, N/P Only

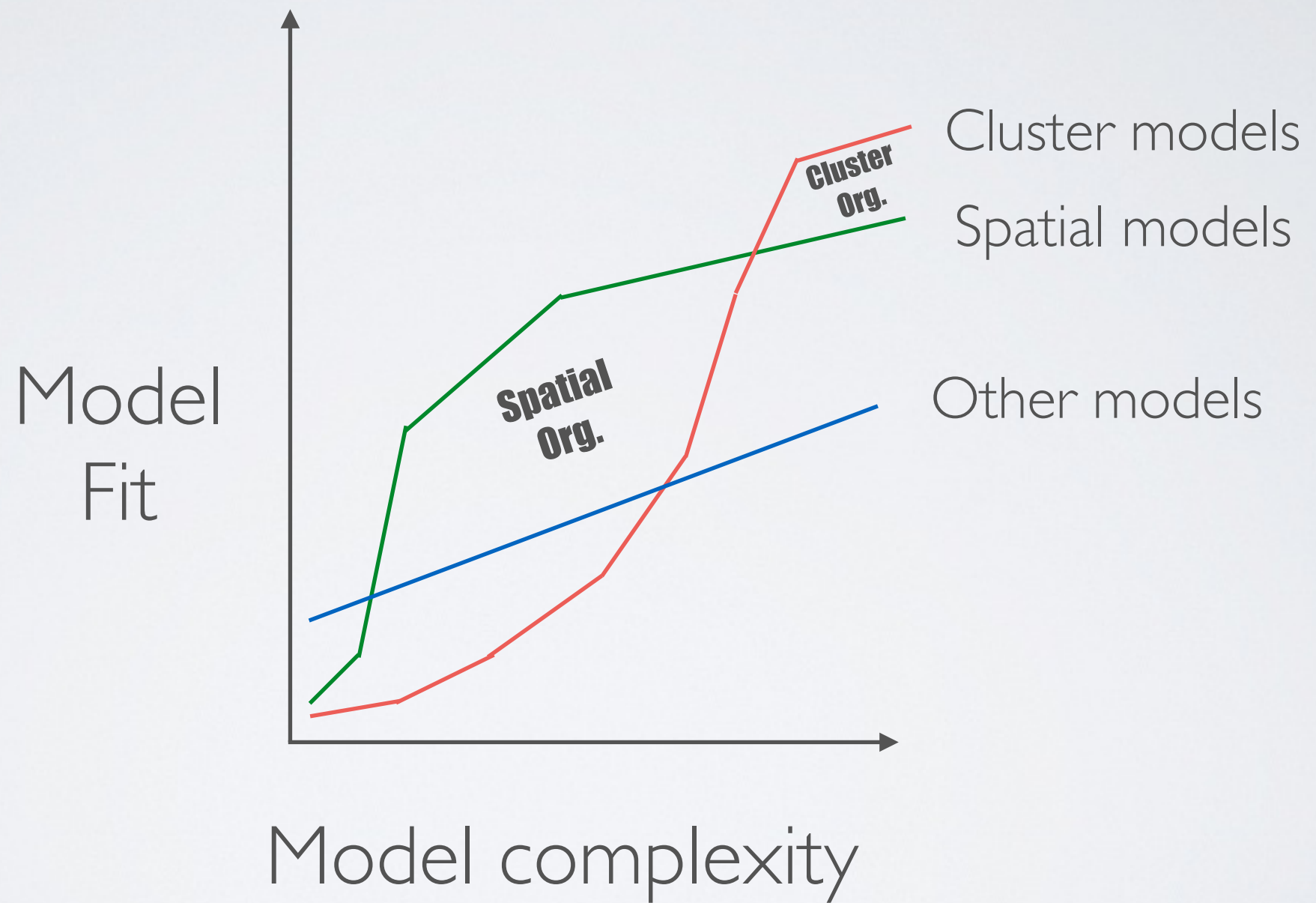


(f) $f(x) = 1/x^{0.5}$, N/P Only

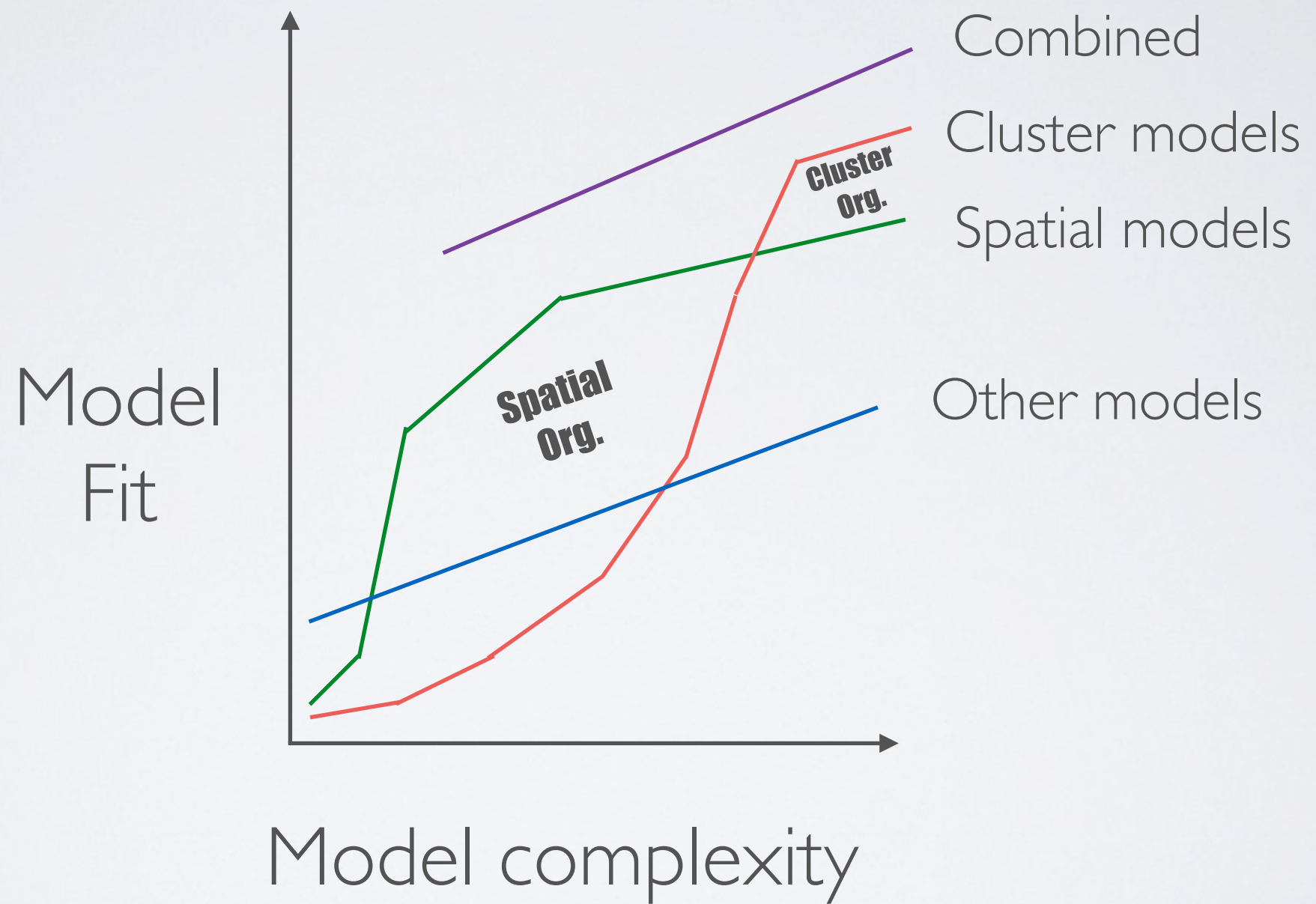
TAKE-HOME MESSAGE

- Complex systems organisation can often be modelled by networks
- Different network models exist
- Complex networks can probably be explained by a combination of factors, i.e. a combination of models

FUTURE WORK (HOPEFULLY)



FUTURE WORK (HOPEFULLY)



THANK YOU
FOR YOUR ATTENTION

PROPOSED NULL MODEL

- **Problem:** Does not conserve degrees !
 - Central nodes have higher degrees
 - Those at the periphery have lower ones.

